WINDS OF HOT MASSIVE STARS

I Lecture: Hot massive stars and stellar winds

¹Brankica Šurlan

¹Astronomical Institute Ondřejov

Selected Topics in Astrophysics

Faculty of Mathematics and Physics October 9, 2013 Prague

- Overview of the course
- Basic properties of hot massive stars
- Importance of hot massive star research
- Signature of stellar mass loss
- How to release the matter from the surface of the star?
- Basic wind types and their driving mechanisms



Overview of the course

First block

Hot massive stars and stellar winds

- Basic properties of hot massive stars
- Importance of hot massive star research
- Signature of stellar mass loss
- How to release the matter from the surface of the star?
- Basic wind types and their driving mechanisms

Second block

Basic wind theory of hot massive stars

- Properties of winds of hot massive stars
- Line-driven wind theory
- The radiative force
- Sobolev approximation
- Wind hydrodynamics equations
- Wind instabilities

Overview of the course

Third block

Quantitative spectroscopy of winds of hot massive stars

- Spectral diagnostics of stellar winds
- P Cygni line profile formation
- Photospheric parameters determination
- Terminal velocity determination
- Mass-loss rates determination
- The Wind-momentum Luminosity Relation (WLR)

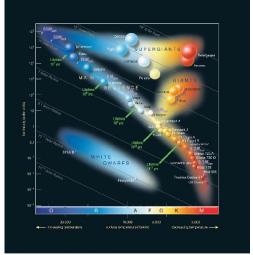
Fourth block

Wind inhomogeneities (clumping)

- Small and large scale structure
- Theoretical predictions
- Observational evidence
- Theoretical wind-models (parametric description of clumped medium)
- Influence of clumping on empirical and predicted mass-loss rates
- Open questions

- EXTREMELY LUMINOUS AND BRIGHT spectral types A, B, and O; $L \gtrsim 10^2 \, [\mathrm{L}_\odot]$ W-R, LBV, B[e] stars
- HOT $T_{\rm eff} \gtrsim 8000 \, [{
 m K}]$
- MASSIVE $M \gtrsim 2 [\mathrm{M}_{\odot}]$

H-R diagram



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Typical parameters for O-type stars

Parameter	Sun	O-type stars
$M [{ m M}_{\odot}]$	1	≥ 8
$T_{\rm eff}[{ m K}]$	6000	≥ 30 000
$L\left[\mathrm{L}_{\odot} ight]$	1	$\sim 10^{6}$
total life time [yr]	10^{10}	$\sim 10^{7}$
$T_{wind}[K]$	10^{6}	$\sim 10^4$
$\dot{M}[M_{\odot} \ yr^{-1}]$	10^{-14}	$\sim 10^{-6}$
$v_{\infty}[\mathrm{km}\mathrm{s}^{-1}]$	400 (700)	$\sim 10^2 - 10^3$

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- VERY RARE
- SMALL FRACTION OF THE STELLAR POPULATION

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ALL OF THEM LOSE THEIR MASS

NGC 602 (Hubble image) IMPORTANCE OF HOT MASSIVE STARS RESEARCH o can be seen at large distances (distance indicators)

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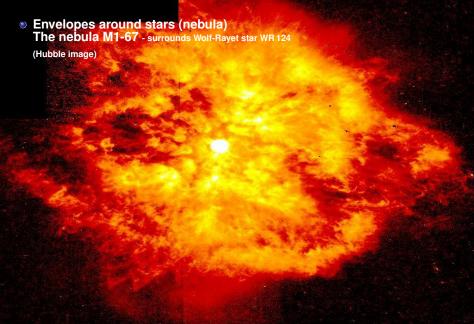
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- stellar winds can be used as a physical laborat

 Envelopes around stars (nebula)
 Abell 39 - planetary nebula in the constellation of Hercules (created by WIYN/NOAO/NSF)





- Envelopes around stars (nebula)
- Interstellar medium (star clusters)
 - PLEIADES open star cluster containing middle-aged hot B-type stars located in the constellation of Taurus (color-composite image from the Digitized Sky Survey)

- Envelopes around stars (nebula)
- Interstellar medium (star clusters)
 - M 17 REGION Omega or Swan Nebula, HII region-molecular cloud. The visible nebula is illuminated by the massive stellar cluster NGC 6618 (ISAAC, VLT ANTU)

- Envelopes around stars (nebula)
- Interstellar medium (bubbles, super bubbles)
 - N 70 nebula (in LMC) (FARS2, ESO)

- Envelopes around stars (nebula)
- Interstellar medium (star clusters)
- Heavier elements (C, N, O, Fe, 7.1)
 - Crab nebula expanding remnant offa superitova explosion (Hubble image

- envelopes around stars (nebula)
- interstellar medium (star clusters)
- heavier elements (C, N, O, Fe, . . .)

WHAT IS SIGNATURE OF STELLAR MASS LOSS?

- envelopes around stars (nebula)
- interstellar medium (star clusters)
- heavier elements (C, N, O, Fe, . . .)

Where do heavier elements come from? ⇒ Fusion reactions in stars

How did heavier elements get into the interstellar medium? ⇒ Must be a way in which the stars loss their mass

- spherically symmetric outflow
- equation of motion

$$\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial r} = g_e - \frac{1}{\rho} \frac{\partial p}{\partial r} - \frac{GM_*}{r^2}$$

- \bullet ρ density
- v radial velocity

$$\frac{\mathrm{d}v(r,t)}{\mathrm{d}t} = \frac{\partial v(r,t)}{\partial t} + \underbrace{\frac{\mathrm{d}r(t)}{\mathrm{d}t}}_{n} \frac{\partial v(r,t)}{\partial r}$$

- p pressure
- g_e external acceleration

- spherically symmetric outflow
- equation of motion

$$\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial r} = \underbrace{g_e}_{\substack{\text{external} \\ \text{acceleration}}} - \underbrace{\frac{\partial p}{\rho \partial r}}_{\substack{\text{gas} \\ \text{pressure} \\ \text{gradient} \\ \text{acceleration}}}_{\substack{\text{gravitational} \\ \text{acceleration}}} - \underbrace{\frac{GM_*}{r^2}}_{\substack{\text{gravitational} \\ \text{acceleration}}}$$

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- equation of motion stationary $\partial/\partial(t) = 0$, i.e time-independent

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- spherically symmetric outflow
- equation of motion stationary $\partial/\partial(t) = 0$, isothermal T(r)=T=const.

$$v\frac{\mathrm{d}v}{\mathrm{d}r} = g_e - \frac{a^2}{\rho}\frac{\mathrm{d}\rho}{\mathrm{d}r} - \frac{GM_*}{r^2}$$

ideal gas equation of state

$$p = \frac{k_B T \rho}{m_H \mu} = a^2 \rho$$

- k_R Boltzmann const.
- m_H mass of hydrogen
- ullet μ mean molecular weight per free gas particles
- isothermal speed of sound (const. for isothermal outflow)

$$a = \sqrt{\frac{k_B T}{m_H \mu}}$$



- spherically symmetric outflow
- equation of motion stationary, isothermal
- integration from R_* to ∞

$$\int\limits_{\mathrm{R}_*}^{\infty} v \, \frac{\mathrm{d}v}{\mathrm{d}r} \, \mathrm{d}r = \int\limits_{\mathrm{R}_*}^{\infty} g_e \, \mathrm{d}r - \int\limits_{\mathrm{R}_*}^{\infty} \frac{a^2}{\rho} \frac{\mathrm{d}\rho}{\mathrm{d}r} \, \mathrm{d}r - \int\limits_{\mathrm{R}_*}^{\infty} \frac{GM_*}{r^2} \, \mathrm{d}r$$

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$$\frac{1}{2}v_{\infty}^{2} - \frac{1}{2}v_{0}^{2} = \int_{R_{*}}^{\infty} g_{e} \, dr - a^{2} \ln \frac{\rho_{\infty}}{\rho_{0}} - \frac{GM_{*}}{R_{*}}$$

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- Two cases:
 - if acting force is large enough

$$\int_{\mathsf{R}_{+}}^{\infty} g_{e} \, \mathsf{d}r \geq \frac{GM_{*}}{\mathsf{R}_{*}}$$

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- Two cases:
 - if acting force is large enough
 - sufficiently high initial velocity v_0

$$\frac{1}{2}v_0^2 \geq \frac{GM_*}{\mathsf{R}_*}$$

• condition for energy: $E_k + E_p \ge 0$



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- integration from R_∗ to ∞

$$\frac{1}{2}v_{\infty}^{2} - \frac{1}{2}v_{0}^{2} = \int_{\mathbf{R}_{*}}^{\mathbf{G}} g_{e} \, \mathrm{d}r - \frac{GM_{*}}{\mathbf{R}_{*}}$$

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$$v_0 \ge v_{\rm esc} = \sqrt{\frac{2GM_*}{R_*}}$$

v_{esc} - escape velocity



- spherically symmetric outflow
- integration from R_∗ to ∞

$$\frac{1}{2}v_{\infty}^2 - \frac{1}{2}v_0^2 = \int\limits_{{\bf R}_*}^{\bf G} g_e \, {\rm d}r - \frac{GM_*}{{\bf R}_*}$$

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- v_{esc} escape velocity
- speed of the particles must be sufficiently large

$$v_{\rm esc} = 620 \,\mathrm{km} \,\mathrm{s}^{-1} \left(\frac{M_*}{\mathrm{M}_\odot}\right)^{1/2} \left(\frac{R_*}{\mathrm{R}_\odot}\right)^{-1/2}$$

How to release the matter from the surface of the star?

- STELLAR WINDS continuous outflow of particles (neutral or charged gas) ejected from the upper atmosphere of a star
 - CORONAL STELLAR WINDS driven by gas pressure due to a high temperature of the gas (solar-type stars)
 - DUST DRIVEN STELLAR WINDS (continuum driven winds) driven by absorption of photons by dust grains (cool luminous stars)
 - LINE DRIVEN STELLAR WINDS driven by absorption in spectral lines (hot massive stars)

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2. EXPLOSION PROCESSES

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- MASS-LOSS RATE \dot{M} [M_{\odot} yr⁻¹]
 - Stationary spherically symmetric wind

$$\dot{M} \equiv \frac{\mathrm{d}M_*}{\mathrm{d}t} = 4\pi r^2 \rho(r) v(r)$$

• TERMINAL VELOCITY - v_{∞} [km s⁻¹] $v_{\infty} = v(r \rightarrow \infty)$

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L. Biermann, 1950 - the "corpuscular" radiation from the Sun may play an important role in forming the radially pointing comet tails

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United States Air Force, photo by Senior Airman Joshua Strang

- CORONAL WINDS the supersonic outflow of electrically charged particles (mainly electrons and protons) from the solar CORONA
- EXPERIMENTAL VERIFICATION observations by LUNA-1,2,3 (1959),
 VENERA 1 (1961), MARINER II (1962), ULYSSES (1990), SOHO (1995)
 - varies in density, temperature, and speed over time and over longitude
 - two components: the slow solar wind ($v \sim 400 \; {\rm km \, s^{-1}}$); the fast solar wind ($v \sim 750 \; {\rm km \, s^{-1}}$)
 - concentration (r= 1 AU) $\sim 10^{-7}$ particles m^{-3} ; $\dot{M} \approx 2 \times 10^{-14}$ M_o yr⁻¹

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WHAT DRIVES THE SOLAR WIND?

GAS PRESSURE DUE TO HIGH TEMPERATURE OF CORONA



Root mean square speed of particles of ideal gas

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What accelerate particles of the Sun?



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- Imbalance between the pressure in the outer corona and the local interstellar medium would lead to an expansion of the coronal gas into a supersonic solar wind
- Parker's solar wind theory has formed the basis for our understanding of the different kinds of the outflows (expanding solar corona, the outflow of ionized gas from galaxies and stars)

Assumption: isothermal spherically symmetric wind

The continuity equation

$$\frac{\partial \rho}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \rho \, v) = 0$$

The equation of motion

$$\rho \frac{\partial v}{\partial t} + \rho v \frac{\partial v}{\partial r} = -a^2 \frac{\partial \rho}{\partial r} - \frac{\rho GM}{r^2}$$

- $\rho(r)$ density
- v(r,t) radial velocity
- a isothermal speed of sound

Assumption: stationary, isothermal spherically symmetric wind

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The continuity equation

$$\frac{\partial \rho}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \rho v) = 0 \implies \dot{M} \equiv 4 \pi r^2 \rho v$$

Assumption: stationary, isothermal spherically symmetric wind

The equation of motion

$$v\frac{\mathrm{d}v}{\mathrm{d}r} = -\frac{a^2}{\rho} \frac{\mathrm{d}\rho}{\mathrm{d}r} - \frac{GM}{r^2}$$

 density gradient expressed by a velocity gradient (follows from equation of continuity)

$$\frac{1}{\rho} \frac{\mathrm{d}\rho}{\mathrm{d}r} = -\frac{1}{v} \frac{\mathrm{d}v}{\mathrm{d}r} - \frac{2}{r}$$

Assumption: stationary, isothermal spherically symmetric wind

The equation of motion

$$\frac{1}{v}(v^2 - a^2)\frac{dv}{dr} = \frac{2a^2}{r} - \frac{GM}{r^2}$$

• critical point $\Rightarrow v(r) = a$ or dv/dr = 0

$$r_{\rm c} = \frac{GM}{2a^2}$$

- singularity at the point where v(r) = a sonic point \Rightarrow $dv/dr \rightarrow \infty$ or $r = r_c$
- for isothermal wind $r_c > r_0$ (r_0 bottom of the isothermal region) and the critical point coincides with the sonic point
- The only solution which can have a positive velocity gradient at all distances is the one that goes through the critical point - Critical solution



Assumption: stationary, isothermal spherically symmetric wind

The equation of motion

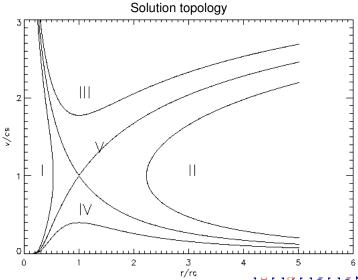
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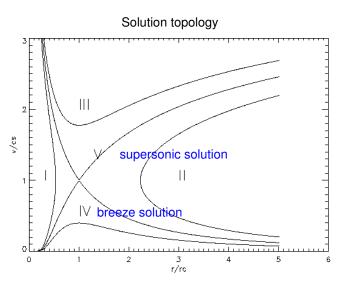
Direct integration yields the general solution

$$F(r, v) \equiv \frac{v^2}{a^2} - \ln \frac{v^2}{a^2} - 4 \ln \frac{r}{r_c} - \frac{4r}{r_c} = C$$

C - integration constant

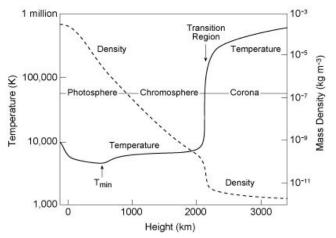






Coronal Heating Problem

Temperature stratification of solar atmosphere



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 - the temperature increases very steeply from chromosphere to the corona
 - corona has very low density

 only a small fraction of the total solar radiation is required to power the corona

Coronal Heating Problem

- Temperature stratification of solar atmosphere
 - the temperature increases very steeply from chromosphere to the corona
 - \bullet corona has very low density \Rightarrow only a small fraction of the total solar radiation is required to power the corona
- How the energy is transported up to the corona, and what mechanism is responsible for the transport?
- several different mechanisms of powering the corona have been proposed:
 - acoustic waves
 - fast and slow magneto-acoustic waves
 - Alfven waves
 - slow and fast magneto-acoustic surface waves
 - current (or magnetic field) dissipation
 - microflares/transients
 - mass/particle flows and magnetic flux emergence
 - "magnetic carpet"
- There is no definite answer to that question yet



- \bullet Luminous cool stars ($L=10^4-10^6\,L_{\odot})$ also have stellar winds. Important for:
 - stars with $0.4\,{\rm M}_\odot \lesssim M_0 \lesssim 8\,{\rm M}_\odot$ (AGB stars $L \le 10^4\,{\rm L}_\odot$ and giant)
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- Doppler effect is not important



Assumption: isothermal spherically symmetric wind

The continuity equation

$$\frac{\partial \rho}{\partial t} + \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \rho \, v) = 0$$

$$\rho \, \frac{\partial v}{\partial t} + \rho \, v \frac{\partial v}{\partial r} = -a^2 \, \frac{\partial \rho}{\partial r} - \frac{\rho \, GM}{r^2} + \underbrace{\rho \, g_{\rm rad}}_{\text{radiation force}} \label{eq:radiation force}$$

- $\rho(r)$ density
- v(r, t) radial velocity
- a isothermal speed of sound
- g_{rad} radiation acceleration

Assumption: isothermal spherically symmetric wind, stationary

The continuity equation

$$\frac{1}{r^2}\frac{\mathsf{d}}{\mathsf{d}r}(r^2\,\rho\,v)=0$$

$$\rho v \frac{\mathrm{d}v}{\mathrm{d}r} = -a^2 \frac{\mathrm{d}\rho}{\mathrm{d}r} - \frac{\rho GM}{r^2} + \rho g_{\text{rad}}$$

Assumption: stationary, isothermal spherically symmetric wind

The continuity equation

$$\frac{1}{r^2}\frac{d}{dr}(r^2\rho v) = 0 \implies \dot{M} \equiv 4\pi r^2\rho v = \text{const.}$$

Assumption: stationary, isothermal spherically symmetric wind

The equation of motion

$$v\frac{\mathrm{d}v}{\mathrm{d}r} = -\frac{a^2}{\rho}\,\frac{\mathrm{d}\rho}{\mathrm{d}r} - \frac{GM}{r^2} + g_{\mathrm{rad}}$$

density gradient expressed by a velocity gradient (equation of continuity)

$$\frac{2}{r} + \frac{1}{v} \frac{dv}{dr} + \frac{1}{\rho} \frac{d\rho}{dr} = 0$$

Assumption: stationary, isothermal spherically symmetric wind

$$\frac{1}{v}(v^2 - a^2)\frac{dv}{dr} = \frac{2a^2}{r} - \frac{GM}{r^2} + g_{\text{rad}}$$

Assumption: stationary, isothermal spherically symmetric wind

The equation of motion

$$\frac{1}{v}(v^2 - a^2)\frac{\mathrm{d}v}{\mathrm{d}r} = \frac{2a^2}{r} - \frac{GM}{r^2} + g_{\text{rad}}$$

• wind is typically cold, $a^2 \ll GM/r \implies$ negligible

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$$\frac{1}{v}(v^2 - a^2)\frac{\mathrm{d}v}{\mathrm{d}r} = -\frac{GM}{r^2} + g_{\text{rad}}$$

• sound point: v = a

$$g_{\text{rad}} = \frac{GM}{r^2}$$

• the radiation force is equal to the gravitational force

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$$g_{\text{rad}} = \frac{GM}{r^2}$$

• subsonic wind: v < a

$$g_{\text{rad}} < \frac{GM}{r^2}$$

• the radiation force is lower than the gravitational force (close to the star)



Assumption: stationary, isothermal spherically symmetric wind

The equation of motion

$$\frac{1}{v}(v^2 - a^2)\frac{\mathrm{d}v}{\mathrm{d}r} = -\frac{GM}{r^2} + g_{\text{rad}}$$

• sound point: v = a

$$g_{\text{rad}} = \frac{GM}{r^2}$$

• subsonic wind: v < a

$$g_{\text{rad}} < \frac{GM}{r^2}$$

• supersonic wind: v > a

$$g_{\text{rad}} > \frac{GM}{r^2}$$

• the radiation force is greater than the gravitational force (far from the star)

$$f_{\text{rad}} = \rho g_{\text{rad}} = \frac{1}{c} \int_{0}^{\infty} \chi(r, \nu) F(r, \nu) d\nu$$

- f_{rad} radiation force
- g_{rad} radiation acceleration
- χ(r, ν) opacity (absorption coefficient)
- F(r, v) radiation flux

Spherically symmetric case

$$g_{\text{rad}} = \frac{1}{c} \int_{0}^{\infty} \kappa(r, \nu) F(r, \nu) \, d\nu$$

• $\kappa = \chi(r, \nu)/\rho$ - changes depending on r only due to changes in the relative concentration of dust

$$g_{\text{rad}} = \frac{F(r)}{c} \int_{0}^{\infty} \kappa(r, \nu) \frac{F(r, \nu)}{F(r)} d\nu$$

- $F(r) = \int_{0}^{\infty} F(r, \nu) d\nu$ total radiation flux
- F(r, v)/F(r) depends only on frequency

$$g_{\text{rad}} = \frac{F(r)}{c} \underbrace{\int\limits_{0}^{\infty} \kappa(r, \nu) \frac{F(r, \nu)}{F(r)} \, d\nu}_{\text{flux mean opacity } \bar{\kappa}(r)}$$

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•
$$L = 4 \pi r^2 F(r)$$

$$g_{\rm rad} = \frac{\bar{\kappa}(r) L}{4 \pi r^2 c}$$



Assumption: isothermal spherically symmetric wind

$$\frac{1}{v}(v^2 - a^2)\frac{dv}{dr} = -\frac{GM}{r^2} + g_{\text{rad}}$$
$$g_{\text{rad}} = \frac{\bar{\kappa}(r)L}{4\pi r^2 c}$$

Assumption: isothermal spherically symmetric wind

The equation of motion

$$\frac{1}{v}(v^2 - a^2)\frac{dv}{dr} = -\frac{GM}{r^2}\left(1 - \frac{\bar{\kappa}(r)L}{4\pi cGM}\right)$$
$$\Gamma_d(r) = \frac{\bar{\kappa}(r)L}{4\pi cGM}$$

• $\Gamma_d(r)$ - ratio of radiative acceleration and gravity



Assumption: isothermal spherically symmetric wind

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- subsonic wind: $\Gamma_d(r) < 1$
- sonic point: $\Gamma_d(r) = 1$
- supersonic wind: $\Gamma_d(r) > 1$
- close to the star (in the atmosphere) there is a little dust, at larger distances leads to its condensation \Rightarrow $\Gamma_d(r)$ increases with radius

The necessary conditions for driving winds with dust

Transfer of momentum from photons to dust grains.



- Transfer of momentum from photons to dust grains.
- The momentum coupling between the grains and the gas (drag force). The driving is produced by the drift of the grains through the gas.
 - sets a lower limit on the mass loss rate that can be driven $(10^{-7} M_{\odot} \text{ yr}^{-1})$
 - sets a limit to the speed of a dust driven wind

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- Radiation field and T determine whether grains form, and at what distance from the star. Density of the dust forming region determines the mass loss rate of the wind.
- Properties of dust opacity determine the transition to supersonic flow and radiative acceleration.